

## PART 2 OF TUTORIAL ON EXTREMES TOOLKIT

### (1) *Using Covariates in Extremes Toolkit*

#### *Simulation from GEV distribution with trend*

##### (i) *Simulate data*

#### **File/Simulate Data/Generalized Extreme Value (GEV)**

GEV parameters:

Location parameter ( $\mu$ ): **0**

Scale parameter ( $\sigma$ ): **1**

Shape parameter ( $\xi$ ): **0.2**

Trend (in location parameter): **0.01**

Sample size: **100**

Save as: `gevtrend.R`

Click on **Generate**

Note: Creates `extRemes` data object `gevtrend.R`

##### (ii) *Fit GEV with no trend to simulated data*

#### **Analyze/Generalized Extreme Value (GEV) Distribution**

Data Object: `gevtrend.R`

Optimization Method: **Nelder-Mead**

Response: `gev.sim`

Plot diagnostics: **check**

Click on **OK**

Note: Fitted output saved in `gev.fit1`

(iii) *Fit GEV with linear trend in location parameter to simulated data*

**Analyze/Generalized Extreme Value (GEV) Distribution**

Data Object: `gevtrend.R`

Optimization Method: **Nelder-Mead**

Response: `gev.sim`

Location parameter (mu): **obs**

Link: **identity**

Plot diagnostics: **check**

Click on **OK**

Note: Fitted output saved in `gev.fit2`

(iv) *Perform likelihood-ratio test for trend in location parameter*

**Analyze/Likelihood-ratio test**

Data Object: `gevtrend.R`

Significance level (alpha): **0.05**

Select base fit (M0): `gev.fit1`

Select comparison fit (M1): `gev.fit2`

Click on **OK**

## (2) *Climate Change Applications*

### (2.1) *Block maxima approach*

#### (2.1.1) *Port Jervis winter maximum temperature (fitting GEV distribution with Arctic Oscillation as covariate)*

To obtain more information about this data set, use R command: `help(HEAT)`

(i) Read data file `PORTw.R` into `extRemes`

#### **File/Read Data**

Select file `PORTw.R`

File Type: **R source**

Save as (in R): `PORTw.R`

Click on **OK**

Note: Creates `extRemes` data object `PORTw.R`

(ii) *Check data*

#### **Plot/Scatter Plot**

Select file `PORTw.R`

Select **points** option

x-axis variable: `AOindex`

y-axis variable: `TMX1`

Click on **OK**

(iii) *Fit GEV with no covariates to maximum temperature data*

**Analyze/Generalized Extreme Value (GEV) Distribution**

Data Object: PORTw.R

Optimization Method: **Nelder-Mead**

Response: TMX1

Plot diagnostics: **check**

Click on **OK**

Note: Fitted output saved in `gev.fit1`

(iv) *Fit GEV with location parameter depending on Arctic Oscillation*

**Analyze/Generalized Extreme Value (GEV) Distribution**

Data Object: PORTw.R

Optimization Method: **Nelder-Mead**

Response: TMX1

Location parameter (mu): AOindex

Link: **identity**

Plot diagnostics: **check**

Click on **OK**

Note: Fitted output saved in `gev.fit2`

(v) *Perform likelihood-ratio test for dependence of location parameter on AO*

**Analyze/Likelihood-ratio test**

Data Object: PORTw.R

Significance level (alpha): **0.05**

Select base fit (M0): `gev.fit1`

Select comparison fit (M1): `gev.fit2`

Click on **OK**

(vi) *Fit GEV with dependence of both location parameter and log(scale parameter) on AO*

**Analyze/Generalized Extreme Value (GEV) Distribution**

Data Object: PORTw.R

Optimization Method: **Nelder-Mead**

Response: TMX1

Location parameter (mu): AOindex

Link: **identity**

Scale parameter (sigma): AOindex

Link: **log**

Plot diagnostics: **check**

Click on **OK**

Note: Fitted output saved in `gev.fit3`

(vii) *Perform likelihood-ratio test for dependence of log(scale parameter) on AO*

**Analyze/Likelihood-ratio test**

Data Object: PORTw.R

Significance level (alpha): **0.05**

Select base fit (M0): `gev.fit2`

Select comparison fit (M1): `gev.fit3`

Click on **OK**

(2.1.2) *Phoenix summer minimum temperature (trend)*

To obtain more information about this data set, use R command: `help(HEAT)`

(i) *Read Phoenix data into extRemes*

**File/Read Data**

Select file HEAT.R

File Type: **R source**

Save as (in R): HEAT.R

Click on **OK**

Note: Creates extRemes data object HEAT.R

(ii) *Check data*

**Plot/Scatter Plot**

Select file HEAT.R

Select **line** option

x-axis variable: Year

y-axis variable: Tmin

Click on **OK**

(iii) *Negate minimum temperature*

**File/Transform Data/Negative**

Data Object: HEAT.R

Variables to Transform: Tmin

Click on **OK**

Note: Creates new variable Tmin.neg

(iv) *Transform time variable*

**File/Transform Data/Affine Transformation**

Data Object: HEAT.R

Variables to Transform: Year

c (subtract): **47**

b (divide by): **1**

Click on **OK**

Note: Creates new variable Year.c47b1

(v) *Fit GEV with no trend to negated data*

**Analyze/Generalized Extreme Value (GEV) Distribution**

Data Object: HEAT.R

Optimization Method: **Nelder-Mead**

Response: Tmin.neg

Plot diagnostics: **check**

Click on **OK**

Note: Fitted output saved in gev.fit1

(vi) *Fit GEV with linear trend in location parameter to negated data*

**Analyze/Generalized Extreme Value (GEV) Distribution**

Data Object: HEAT.R

Optimization Method: **Nelder-Mead**

Response: Tmin.neg

Location parameter (mu): Year.c47b1

Link: **identity**

Plot diagnostics: **check**

Click on **OK**

Note: Fitted output saved in gev.fit2

(vii) *Perform likelihood-ratio test for trend in location parameter*

**Analyze/Likelihood-ratio test**

Data Object: HEAT.R

Significance level (alpha): **0.05**

Select base fit (M0): gev.fit1

Select comparison fit (M1): gev.fit2

Click on **OK**

(viii) *Fit GEV with linear trends in both location parameter and log(scale parameter) to negated data*

**Analyze/Generalized Extreme Value (GEV) Distribution**

Data Object: HEAT.R

Optimization Method: **Nelder-Mead**

Response: Tmin.neg

Location parameter (mu): Year.c47b1

Link: **identity**

Scale parameter (sigma): Year.c47b1

Link: **log**

Plot diagnostics: **check**

Click on **OK**

Note: Fitted output saved in gev.fit3

(ix) *Perform likelihood-ratio test for trend in log(scale parameter)*

**Analyze/Likelihood-ratio test**

Data Object: HEAT.R

Significance level (alpha): **0.05**

Select base fit (M0): gev.fit2

Select comparison fit (M1): gev.fit3

Click on **OK**

(2.3) *Point process model (Fort Collins daily precipitation with annual cycle in location parameter)*

(i) *Create cosine and sine variables*

#### **File/Transform Data/Trigonometric Transformation**

Data Object: FtCoPrec.R

Period: **365.25**

Variables to Transform: obs

Click on **OK**

Note: Creates new variables obs.sin365 and obs.cos365

(ii) *Fit point process with annual cycle in location parameter*

#### **Analyze/Point Process Model**

Data Object: FtCoPrec.R

Response: Prec

Location parameter (mu): obs.sin365 and obs.cos365

Link: **identity**

Plot diagnostics: **uncheck**

Method: **Nelder-Mead**

Threshold: **0.395**

Number of obs per year: **365.25**

Click on **OK**

Note: Fitted output saved in pp.fit2

(iii) *Perform likelihood-ratio test for annual cycles in location parameter*

#### **Analyze/Likelihood-ratio test**

Data Object: FtCoPrec.R

Significance level (alpha): **0.05**

Select base fit (M0): pp.fit1

Select comparison fit (M1): pp.fit2

Click on **OK**